

Level - 1

Daily Tutorial Sheet - 6

$$76.(B) \quad F(t) = \int_0^t e^{(t-y)} \cdot y dy = e^t \int_0^t y e^{-y} dy = e^t \left[-e^{-y}(y+1) \right]_0^t = e^t [1 - e^{-t}(t+1)] = e^t - (t+1)$$

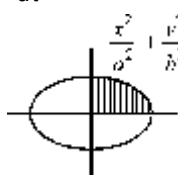
77.(D)

$$78.(ABCD) \quad f'(x) = \left(\frac{x^4 - 5x^2 + 4}{2 + e^{x^2}} \right) 2x = \frac{(x^2 - 1)(x^2 - 4)2x}{(2 + e^{x^2})} \geq 0$$

$$79.(ABD) \quad f(x) = \int_0^x |x-1| \quad f'(x) = |x-1| \quad \text{Continuous, Diff at } x=2, \text{ Continuous at } x=1$$

$$80.(C) \quad \frac{dx}{dt} = t \cdot \sec^2 t; \quad \frac{dy}{dt} = \frac{\cos t}{\sqrt{t}} \times \frac{+1}{2\sqrt{t}}; \quad \frac{dy}{dx} = \frac{\cos^3 t}{2t^2}.$$

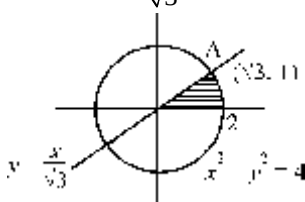
81.



$$\text{Required Area} = 4 \times \text{shaded area} = 4 \int_0^a b \sqrt{1 - \frac{x^2}{a^2}}; \quad dx = \pi ab.$$

82.

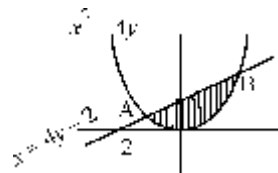
$$\text{Solve } y = \frac{x}{\sqrt{3}} \text{ \& } x^2 + y^2 = 4 \Rightarrow A \equiv (\sqrt{3}, 1)$$



$$\text{Required Area} = \int_0^1 [\sqrt{4-y^2} - \sqrt{3}y] dy = \frac{\pi}{3}$$

$$83. \quad \text{Solve } x^2 = 4y \text{ \& } x = 4y - 2 \text{ to get } A \equiv \left(-1, \frac{1}{4}\right) \text{ \& } B \equiv (2, 1)$$

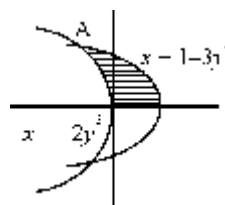
$$\text{Required Area} = \text{Shaded Area} = \int_{-1}^2 \left(\frac{x+2}{4} - \frac{x^2}{4} \right) dx = \frac{9}{8}$$



$$84. \quad \text{Required Area} = 2 \times \text{shaded area} = 2 \int_0^{y_A} [(1-3y^2) - (-2y^2)] dy$$

$$\text{Solve } x = -2y^2 \text{ \& } x = 1-3y^2 \Rightarrow A \equiv (-2, 1)$$

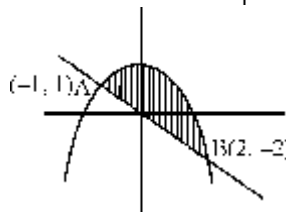
$$\Rightarrow \text{Required Area} = 2 \int_0^1 (1-y^2) dy = 4/3.$$



$$85. \quad \text{To get } A \text{ \& } B, \text{ solve } y = 2-x^2 \text{ and } x+y=0$$

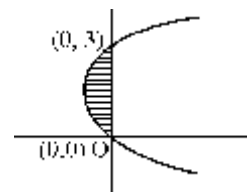
$$\Rightarrow A \equiv (-1, 1) \text{ \& } B \equiv (2, -2)$$

$$\Rightarrow \text{Shaded Area} = \int_{-1}^2 [(2-x^2) - (-x)] dx = \frac{9}{2}$$



86. $y^2 = x + 3y$

$$\Rightarrow \left(y - \frac{3}{2}\right)^2 = x + \frac{9}{4} \Rightarrow \text{Shaded Area} = -\int_0^3 \left[\left(y - \frac{3}{2}\right)^2 - \frac{9}{4} \right] dy = \frac{9}{2}.$$

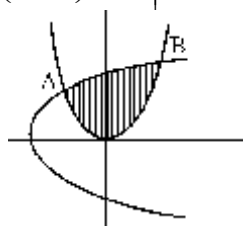


87. To get A & B solve $y^2 = 5x + 6$ & $x^2 = y$

$$\Rightarrow A \equiv (-1, 1) \text{ \& \; } B \equiv (2, 4)$$

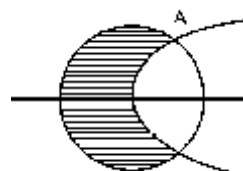
Required Area = Shaded Area

$$= \int_{-1}^2 (\sqrt{5x+6} - x^2) dx = \frac{81}{15} = \frac{27}{5}$$



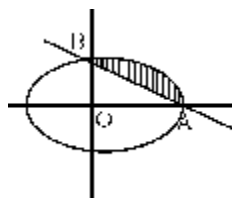
88. Required Area = $\pi \cdot 8^2 - 2 \int_0^{y_A} \left[\sqrt{64 - y^2} - \frac{y^2}{12} \right] dy$

$$= \frac{16}{3} (8\pi - \sqrt{3})$$



89. Shaded Area = $\int_0^a b \sqrt{1 - \frac{x^2}{a^2}} dx - \int_0^a b \left(1 - \frac{x}{a} \right) dx$

$$= \frac{1}{4} ab (\pi - 2)$$



90. Shaded Area = $2 \int_0^{x_A} \left(\frac{2}{1+x^2} - x^2 \right) dx$

Solve $y = \frac{2}{1+x^2}$ & $y = x^2$. $A \equiv (1, 1)$.

$$\Rightarrow \text{Shaded Area} = 2 \int_0^1 \left(\frac{2}{1+x^2} - x^2 \right) dx = \pi - \frac{2}{3}$$

